

## LESSON PLAN 11

**CLASS : 9 SUBJECT : MATHEMATICS TEACHER'S NAME :**

NAME OF THE UNIT	SUB-TOPICS	NO OF PERIODS REQUIRED			Time line for teaching	
		Teaching	Practice	TOTAL	From	To
<b>SURFACE AREAS AND VOLUMES</b>	11.1 SURFACE AREA OF A RIGHT CIRCULAR CONE	2	3	5		
	11.2 SURFACE AREA OF A SPHERE	2	3	5		
	11.3 VOLUME OF A RIGHT CIRCULAR CONE	2	3	5		
	11.4 VOLUME OF A SPHERE	2	3	5		
	TOTAL	8	12	20		

**PRE-REQUISITES  
&  
SKILLS**

Every Pupil is expected to have basic knowledge in

- # visualising solid shapes
- # recognizing the surfaces like lateral surface, curved surface, total surface etc with respect to 3 dimensional objects
- # Formulae related to areas of two dimensional shapes like rectangle, square, circle etc.,
- # basic mathematical operations .

## Learning Outcomes

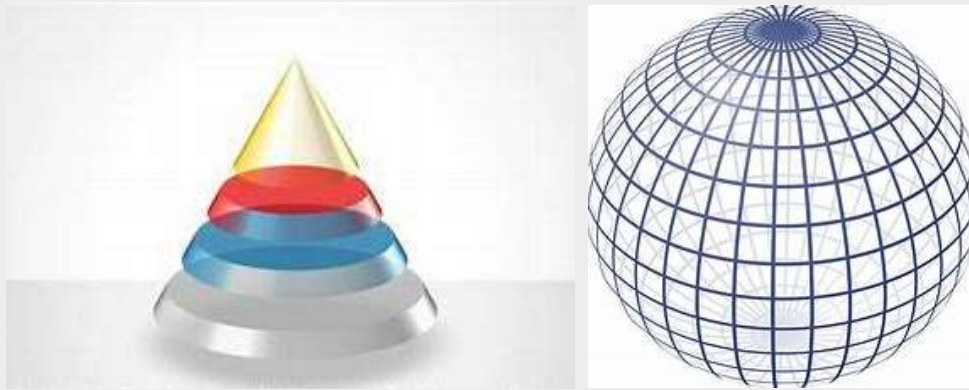
After Completion of this lesson every student will be able to

- # distinguish between area and volume of a three dimensional object
- # arrive at formulae for finding the surface areas and volumes of cone & sphere.
- # calculate the lateral surface area and total surface area of conical and spherical shaped real life objects using the formulae.
- # utilize the formulae of volume of cone and sphere in calculating the volume of these objects in real life situations.
- # appreciate the utility of "SURFACE AREAS AND VOLUMES" in real life sums

## Teaching Learning Process

### INTRODUCTION /INDUCTION

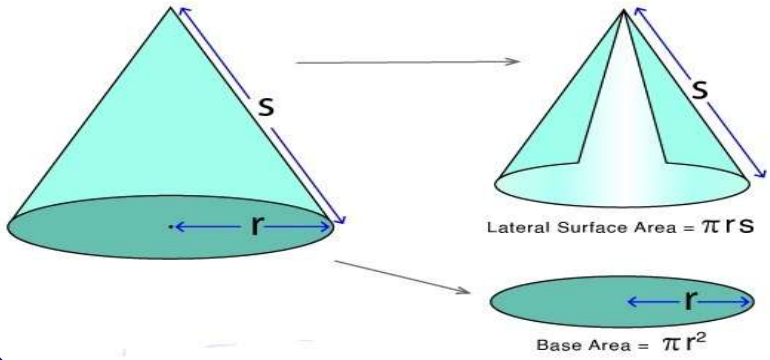
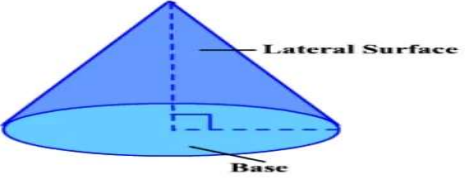
Teacher introduces the chapter of SURFACE AREAS AND VOLUMES by recalling their previous knowledge on areas and volumes of 3 dimensional objects like cuboid, cube, cylinder in their previous class. Teacher briefs that cone can be considered as circular pyramid.



### Experience & Reflection

# Pupils will recollect their knowledge on surface areas and volumes of cuboids, cubes and cylinders and utilize that in exploring, learning and deducing the formulae for surface area and volume of cone and sphere.

# Students will experience the usage of the concept of Surface areas and Volumes and appreciate its usage.

EXPLICIT TEACHING/TEACHER MODELLING (I DO)	GROUP WORK (WE DO)	INDEPENDENT WORK (YOU DO)	NOTES
<p><b>11.1. Surface Area of a right circular cone</b>            Teacher introduces the concept of cone through their previous knowledge on prisms and pyramids and now briefs cone as a circular pyramid. Later teacher guides children arrive at the area of the surface area of cone through an activity.</p>	<p>Pupil groups will be instructed to cut sectors out of a circle paper and twirl the sector along its arc in such a way that the two radii touch along each other. It obviously forms a cone. Now each group will transform each cone into a sector and sub divide the sector into triangles by keeping the slant height of the cone (circle radius) as the the height of the triangle and bases will be parts of the arc. To find the lateral surface area of the cone they add all the areas of the triangles</p>	<p>Every individual will participate in the activity and learn the concept of finding the surface area of a cone</p>	<p>Surface area of a cone formulae</p>
<div data-bbox="134 899 1033 1377" style="border: 2px solid blue; padding: 10px;"> <p style="text-align: center;"><b>Surface Area of a Cone</b></p>  </div>		<div data-bbox="1066 964 1892 1377" style="border: 2px solid green; padding: 10px;"> <p style="text-align: center;"><b>TOTAL SURFACE AREA OF CONE</b></p> <ul style="list-style-type: none"> <li>Total Surface Area of Cone(TSA) =base area+CSA  <math>= \pi r^2 + \pi r l</math>  <math>= \pi r(l+r)</math></li> </ul>  </div>	

$$= \frac{1}{2} b_1 l + \frac{1}{2} b_2 l + \frac{1}{2} b_3 l + \frac{1}{2} b_4 l + \dots$$

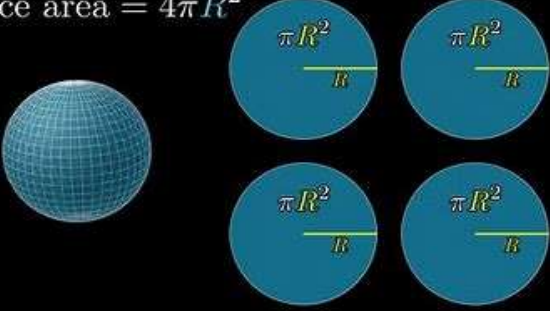
$$= \frac{1}{2} l (b_1 + b_2 + b_3 + b_4 + \dots)$$

$$= \frac{1}{2} l (2\pi r)$$

$$= \pi r l$$

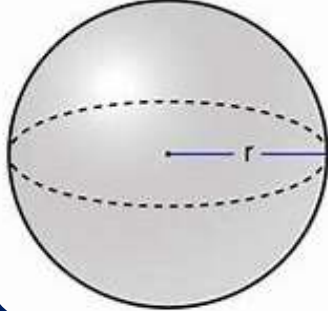
EXPLICIT TEACHING/TEACHER MODELLING (I DO)	GROUP WORK (WE DO)	INDEPENDENT WORK (YOU DO)	NOTES
<p><b>11.2. Surface Area of a Sphere</b> Teacher induces the concept of surface area of a sphere through an activity.</p>	<p>Pupil groups will be given rubber balls along with a thin rope and are instructed to stick the rope in such a way that it covers the entire ball. Then the part of the rope that covers the ball is now arranged to cover the area of circles with equivalent radius of the sphere. This obviously comes to a conclusion that the part of the rope that covered the sphere is equivalent to the area of 4 circles with same radius to that of a sphere</p>	<p>Every individual will participate in the activity and learn the concept of finding the surface area of a sphere</p>	<p>Surface area of a sphere formula</p>

Surface area =  $4\pi R^2$



The diagram shows a blue wireframe sphere on the left. To its right are four blue circles arranged in a 2x2 grid. Each circle has a radius line drawn from the center to the edge, labeled with the letter 'R'. Above each circle is the formula  $\pi R^2$ .

Surface Area of a Sphere



Formula:  
Surface Area (SA) =  $4\pi r^2$

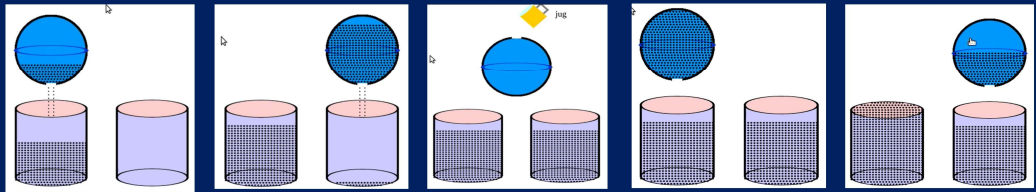
here,  
 $\pi = \frac{22}{7} = 3.141,$   
 $r = \text{radius}$

The diagram shows a grey sphere with a horizontal radius line drawn from the center to the right edge, labeled with the letter 'r'. The sphere is shown with a dashed line for the back part of the equator to indicate its three-dimensional nature.

EXPLICIT TEACHING/TEACHER MODELLING (I DO)	GROUP WORK (WE DO)	INDEPENDENT WORK (YOU DO)	NOTES
<p><b>11.3. Volume of a right circular cone</b></p> <p>Teacher explains the concept of Volume of a cone using laboratory method by engaging children in an activity where groups of children are provided with a cylinder and a cone of equal base radius and height.</p>	<p>Pupil groups will be given a cone and a cylinder with <b>equal base radius and height</b>. Now a heap of sand is also provided and each group is instructed to fill the cylinder with sand using the cone. It obviously end up with 3 complete fillings of a cone makes a completely filled cylinder. Through this teacher guides children to arrive at the volume of cylinder = 3 x volume of cone</p> <div data-bbox="579 857 1136 1284" style="border: 2px solid red; padding: 5px;"> </div>	<p>Every individual will participate in the activity and learn the concept of finding the volume of a cone</p> <div data-bbox="1245 659 1850 1295" style="border: 2px solid green; padding: 5px;"> <p style="text-align: center;"><b>Figura 7</b></p> </div>	<p>Volume of a cone formula</p>

EXPLICIT TEACHING/TEACHER MODELLING (I DO)	GROUP WORK (WE DO)	INDEPENDENT WORK (YOU DO)	NOTES
<p><b>11.4. Volume of a Sphere</b>            Teacher explains the concept of Volume of a sphere using laboratory method by engaging children in an activity where groups of children are provided with 2 cylinders and a sphere of equal radius</p>	<p>Pupil groups will be given a sphere and a cylinder with <b>equal base radius and height</b>. Now a heap of sand is also provided and each group is instructed to fill the cylinder with sand using the sphere. It obviously end up with 3 complete fillings of a sphere make 2 completely filled cylinders. Through this teacher guides children to arrive at the <math>2 \times \text{volume of cylinder} = 3 \times \text{volume of sphere}</math></p>	<p>Every individual will participate in the activity and learn the concept of finding the volume of a sphere</p>	<p>Volume of a sphere formula</p>

### Finding Volume of a sphere using the volume of Cylinder



#### Volume of a sphere

**Workbench**

**Given:**  
 Diameter of sphere =  $2r$   
 Diameter of each cylinder =  $2r$   
 Height of each cylinder ( $h$ ) =  $2r$   
 We have seen that we required three pourings of sand into sphere to fill both the cylinders

**Proof:**  
 Therefore,  
 $3 * (\text{Volume of sphere}) = 2 * (\text{Volume of cylinder})$   
 $3 * (\text{Volume of sphere}) = 2 * (\pi * r^2 * h)$   
 $3 * (\text{Volume of sphere}) = 2 * \pi * r * r * r * 2 \quad (h = 2r)$   
 $\text{Volume of sphere} = \frac{4}{3} * \pi * r^3 \quad (h = 2r)$   
 Hence proved

Hence, we have proved that Volume of a sphere is  $(\frac{4}{3}) * \pi * r * r * r$

**CHECK FOR UNDERSTANDING QUESTIONS**

1. Factual	1) Find the total surface area of a cone, if its slant height is 21 m and diameter of its base is 24 m. 2) The diameter of a metallic ball is 4.2 cm. What is the mass of the ball, if the density of the metal is 8.9 g per $\text{cm}^3$ ?
2. Open Ended/Critical Thinking	1) Twenty seven solid iron spheres, each of radius $r$ and surface area $S$ are melted to form a sphere with surface area $S'$ . Find the (i) radius $r'$ of the new sphere, (ii) ratio of $S$ and $S'$ . 2) A hemispherical bowl is made of steel, 0.25 cm thick. The inner radius of the bowl is 5 cm. Find the outer curved surface area of the bowl.
3. Student Practice questions & Activities	1. A hemispherical bowl made of brass has inner diameter 10.5 cm. Find the cost of tin plating it on the inside at the rate of ₹ 16 per $100 \text{ cm}^2$ 2. A joker's cap is in the form of a right circular cone of base radius 7 cm and height 24 cm. Find the area of the sheet required to make 10 such caps.
4. Assessment	Exercise sums and worksheet on Surface Area & Volumes