

## LESSON PLAN 1

**CLASS : 8** TEACHER'S NAME :

NAME OF THE UNIT	SUB-TOPICS	NO OF PERIODS REQUIRED			Time line for teaching	
		Teaching	Practice	TOTAL	From	To
<b>RATIONAL NUMBERS</b>	1.1 INTRODUCTION	<b>1</b>	<b>7</b>	<b>8</b>		
	1.2 PROPERTIES OF RATIONAL NUMBERS					
	1.2.1 CLOSURE					
	1.2.2 COMMUTATIVITY					
	1.2.3 ASSOCIATIVITY	<b>1</b>	<b>7</b>	<b>8</b>		
1.2.4 THE ROLE OF ZERO						
1.2.5 THE ROLE OF 1						
1.2.6 DISTRIBUTIVITY OF MULTIPLICATION OVER ADDITION FOR RATIONAL NUMBERS	<b>1</b>	<b>7</b>	<b>8</b>			
<b>TOTAL</b>				<b>3</b>	<b>21</b>	<b>24</b>
	<b>KEY CONEPTS</b>	<b>KEY VOCABULARY</b>				
<b>PRE-REQUISITES</b>	Every Pupil is expected to have basic knowledge in # Natural Numbers, Whole Numbers and Integers and fractions # four basic operations like +,-,x and ÷ on fractions # Properties of Closure,Commutative, Associative,Identity, distributivity in the set of integers	# Integers # Natural Numbers # Whole Numbers # Rational Numbers # Fractions			# closure # Commutativity # Associativity # Identity # Distributivity	

## Learning Outcomes

After Completion of this lesson every student will be able to

- # identify the right property utilized in simplifying Rational expressions
- # add, subtract, multiply and divide Rational numbers with ease.
- # utilize the right property in simplification of rational expressions under various operations
- # recognize the significance and appreciate the importance of Rational operations in real life situations.

## Teaching Learning Process

### MIND MAPPING

### Experience & Reflection


## VARIOUS PROPERTIES OF RATIONAL NUMBERS (Q)

OPERATION / PROPERTY	ADDITION	SUBTRACTION	MULTIPLICATION	DIVISION
CLOSURE	YES	YES	YES	NO (YES IF WE EXCLUDE 0)
COMMUTATIVITY	YES	NO	YES	NO
ASSOCIATIVITY	YES	NO	YES	NO
IDENTITY	YES – 0	NO	YES – 1	NO

# Pupils will recollect their knowledge on Fractions and their usage that they were acquainted with in their previous class and will reflect the knowledge here in exploring the properties in Rational Numbers under various operations

# Students will experience the usage of Rational Numbers in real life situations.

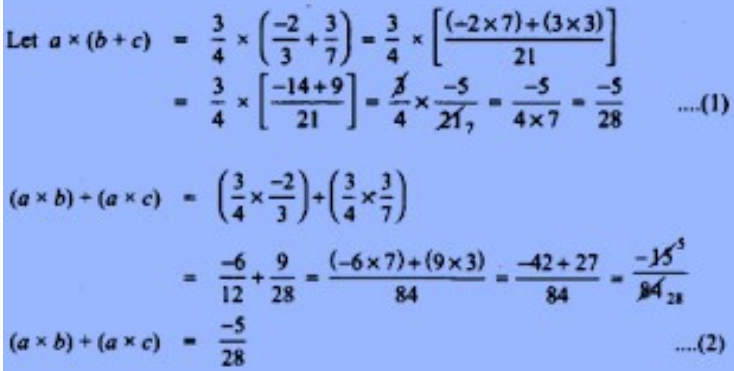
**DISTRIBUTIVITY OF MULTIPLICATION OVER ADDITION IS SATISFIED IN THE SET OF RATIONAL NUMBERS**

TEACHING PERIOD : 1	INTRODUCTION, PROPERTIES OF RATIONAL NUMBERS, CLOSURE, COMMUTATIVITY																										
CONCEPTS/STEPS	TEACHER ACTIVITY (I DO)	GROUP ACTIVITY (WE DO)	INDIVIDUAL ACTIVITY ( YOU DO )																								
KEY WORDS & PRE REQUISITES	Brain storming session involving children with pre-requisites vocabulary and concepts related to previous knowledge. Introduction of new vocabulary and key words associated with the concept # NATURAL NUMBERS # WHOLE NUMBERS # INTEGERS # FRACTIONS # RATIONAL NUMBERS # ADDITION # SUBTRACTION # SUBTRACTION # DIVISION # CLOSURE # COMMUTATIVITY	* Students read the pre-requisites and answer the questions to the teacher (whole class activity)	Every Pupil will read and write the key words in their note books																								
MIND MAPPING	Teacher writes the key word "RATIONAL NUMBERS" on the black board and will elicit its other related words through questioning and will draw pupils' attention towards key concepts in the lesson	Heterogeneous groups are created. One group will read the words and other will explain the meaning	Pupils individually read the keywords associated with Integers																								
CONCEPTUAL UNDERSTANDING	Teacher presents different properties of rationals under Addition, subtraction, multiplication & divisions through recollecting their previous knowledge on these properties in case of whole numbers and integers.	Heterogeneous groups are formed to participate in the activity and each group participates in the activity actively and learn the properties	Each student in the group participates in the activity and learns the properties on Rational numbers																								
LEARNING ACTIVITY	Teacher conducts an activity by dividing children into Heterogeneous groups and will give different rational numbers to each group and asks children to operate them with +, -, ×, ÷ in different orders and check what were the results. Finally Teacher draws inferences from children themselves that Set of Rationals (Q) is Closed under Addition, subtraction, Multiplication and is closed under division if we exclude '0' from the set otherwise not closed.  <div style="display: flex; justify-content: space-around;"> <div data-bbox="520 1047 877 1307"> <p><b>CLOSURE PROPERTY FOR RATIONAL NUMBERS</b></p> <p><b>ADDITION</b> <math>\frac{3}{8} + \left(\frac{-5}{7}\right) = \frac{(21+(-40))}{56} = \frac{-19}{56}</math> Rational</p> <p><b>SUBTRACTION</b> <math>-\frac{6}{7} - \frac{8}{3} = \frac{-18-28}{21} = \frac{-46}{21}</math> Rational</p> <p><b>MULTIPLICATION</b> <math>-\frac{3}{8} \times \frac{4}{5} = \frac{-12}{40}</math> Rational</p> <p><b>DIVISION</b> <math>\frac{-5}{3} \div \frac{2}{7} = \frac{-5 \times 7}{3 \times 2} = \frac{-35}{6}</math> Rational</p> <p>However, <math>\frac{5}{3} \div 0 = 0</math> NOT DEFINED → So, excluding zero, all other rational numbers are closed under division.</p> </div> <div data-bbox="907 1047 1264 1307"> <p><b>COMMUTATIVITY FOR RATIONAL NUMBERS</b></p> <p><b>ADDITION</b>  <math>a+b = \frac{2}{3} + \frac{5}{7} = \frac{14}{21} + \frac{15}{21} = \frac{29}{21}</math>  <math>b+a = \frac{5}{7} + \left(\frac{2}{3}\right) = \frac{10}{21} + \frac{14}{21} = \frac{24}{21}</math>  <math>a+b = b+a</math></p> <p><b>SUBTRACTION</b>  <math>a-b = \frac{2}{3} - \frac{5}{7} = \frac{14}{21} - \frac{15}{21} = \frac{-1}{21}</math>  <math>b-a = \frac{5}{7} - \frac{2}{3} = \frac{15}{21} - \frac{14}{21} = \frac{1}{21}</math>  <math>a-b \neq b-a</math></p> <p><b>MULTIPLICATION</b>  <math>a \times b = \frac{2}{3} \times \frac{5}{7} = \frac{10}{21}</math>  <math>b \times a = \frac{5}{7} \times \left(\frac{2}{3}\right) = \frac{10}{21}</math>  <math>a \times b = b \times a</math></p> <p><b>DIVISION</b>  <math>a \div b = \frac{2}{3} \div \frac{5}{7} = \frac{2 \times 7}{3 \times 5} = \frac{14}{15}</math>  <math>b \div a = \frac{5}{7} \div \left(\frac{2}{3}\right) = \frac{5 \times 3}{7 \times 2} = \frac{15}{14}</math>  <math>a \div b \neq b \div a</math></p> </div> </div>	 <table border="1" style="margin-left: auto; margin-right: auto;"> <caption>Properties of Rational Numbers</caption> <thead> <tr> <th colspan="4">Properties of rational numbers</th> </tr> <tr> <th>Operation</th> <th>Closure property</th> <th>Commutative property</th> <th>Associative property</th> </tr> </thead> <tbody> <tr> <td>+</td> <td>✓</td> <td>✓</td> <td>✓</td> </tr> <tr> <td>-</td> <td>✓</td> <td>✗</td> <td>✗</td> </tr> <tr> <td>×</td> <td>✓</td> <td>✓</td> <td>✓</td> </tr> <tr> <td>÷</td> <td>✓</td> <td>✗</td> <td>✗</td> </tr> </tbody> </table>	Properties of rational numbers				Operation	Closure property	Commutative property	Associative property	+	✓	✓	✓	-	✓	✗	✗	×	✓	✓	✓	÷	✓	✗	✗	
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SUMMARY	Teacher writes the summary of the concept in a tabular form and asks children to note and read	pupils will note down and read the summary in groups	every individual reads the summary and notes it down																								
ASSESSMENT	Teacher asks children to solve the sums of try these section of pg.no: 4,6	every group will do the sums by discussion among each other	every individual solves the sums on their own																								

PRACTICE PERIOD: 1 to 7		INTRODUCTION, PROPERTIES OF RATIONAL NUMBERS, CLOSURE, COMMUTATIVITY	
CONCEPTS/STEPS	TEACHER ACTIVITY (I DO)	GROUP ACTIVITY (WE DO)	INDIVIDUAL ACTIVITY ( YOU DO )
KEY WORDS READING	Teacher writes the key words from previous class's teaching period and asks children to read and write them in note books # NATURAL NUMBERS # WHOLE NUMBERS # INTEGERS # FRACTIONS # RATIONAL NUMBERS # ADDITION # SUBTRACTION # SUBTRACTION # DIVISION # CLOSURE # COMMUTATIVITY	Whole class activity : one child comes to the board and reads the key words loudly and the remaining class follows.	Every child comes to the board and reads the key words and notes them down in their note books
SIMILAR LINES READING	Teacher writes some expressions and writes the property involved in those expressions and asks children to do some more $\frac{1}{8} + \frac{3}{5} = \frac{29}{40}$ closure property under addition $\frac{1}{8} \times \frac{3}{5} = \frac{3}{5} \times \frac{1}{8}$ commutative property under multiplication	Each group will read the similar lines and will frame some more by discussion	Every Individual prepares their own similar lines using the lines prepared by the teacher
SUMMARY/ SYNOPSIS	Teacher once again writes important key words and tabulates different properties of Rationals under Various operations and asks children to read, note down and practice.	pupils will note down and read the summary in groups	every individual spells and reads the summary and notes it down
WRITING/ EDITING	Teacher guides children in doing sums of try these section on their own and checks their writings	One group will check the writings of the other and vice versa	Slow learners are focused and teacher will ascertain that every individual learns the concept in successive upcoming practice sessions

TEACHING PERIOD : 2	ASSOCIATIVITY, THE ROLE OF ZERO, THE ROLE OF 1																											
CONCEPTS/STEPS	TEACHER ACTIVITY ( I DO )	GROUP ACTIVITY ( WE DO )	INDIVIDUAL ACTIVITY ( YOU DO )																									
KEY WORDS	Brain storming session involving children with key words * Associativity * Identity * Inverse	* Students read the keywords answer the questions to the teacher (whole class activity)	Every Pupil will read and write the key words in their note books																									
CONCEPTUAL UNDERSTANDING	<p>Teacher demonstrates the concept of Associativity using previous techniques as it was done in the case of closure and commutativity and further introduces the role of '0' and '1' as identities in Rational Number set as they are familiar with those two numbers which worked as identities in case of whole numbers too under addition and multiplication respectively</p> <table border="1" data-bbox="520 760 1178 1153"> <thead> <tr> <th>LHS</th> <th>RHS</th> <th>Result</th> </tr> </thead> <tbody> <tr> <td><math>\left(\frac{1}{5} + \frac{2}{7}\right) + \frac{1}{3} = \frac{86}{105}</math></td> <td><math>\frac{1}{5} + \left(\frac{2}{7} + \frac{1}{3}\right) = \frac{86}{105}</math></td> <td>The values are equal and they satisfy the condition.</td> </tr> <tr> <td><math>\left(\frac{4}{9} - \frac{3}{2}\right) - \frac{1}{3} = -\frac{93}{57}</math></td> <td><math>\frac{4}{9} - \left(\frac{3}{2} - \frac{1}{3}\right) = -\frac{39}{54}</math></td> <td>The values differ and so subtraction is not associative for rational numbers.</td> </tr> <tr> <td><math>\frac{3}{8} \times \left(\frac{1}{9} \times \frac{5}{7}\right) = \frac{15}{504}</math></td> <td><math>\left(\frac{3}{8} \times \frac{1}{9}\right) \times \frac{5}{7} = \frac{15}{504}</math></td> <td>Multiplication is associative for rational numbers.</td> </tr> <tr> <td><math>\frac{3}{5} \div \left(\frac{2}{5} \div \frac{2}{5}\right) = \frac{3}{5}</math></td> <td><math>\left(\frac{3}{5} \div \frac{2}{5}\right) \div \frac{2}{5} = \frac{15}{4}</math></td> <td>Division is not associative for rational numbers.</td> </tr> </tbody> </table>	LHS	RHS	Result	$\left(\frac{1}{5} + \frac{2}{7}\right) + \frac{1}{3} = \frac{86}{105}$	$\frac{1}{5} + \left(\frac{2}{7} + \frac{1}{3}\right) = \frac{86}{105}$	The values are equal and they satisfy the condition.	$\left(\frac{4}{9} - \frac{3}{2}\right) - \frac{1}{3} = -\frac{93}{57}$	$\frac{4}{9} - \left(\frac{3}{2} - \frac{1}{3}\right) = -\frac{39}{54}$	The values differ and so subtraction is not associative for rational numbers.	$\frac{3}{8} \times \left(\frac{1}{9} \times \frac{5}{7}\right) = \frac{15}{504}$	$\left(\frac{3}{8} \times \frac{1}{9}\right) \times \frac{5}{7} = \frac{15}{504}$	Multiplication is associative for rational numbers.	$\frac{3}{5} \div \left(\frac{2}{5} \div \frac{2}{5}\right) = \frac{3}{5}$	$\left(\frac{3}{5} \div \frac{2}{5}\right) \div \frac{2}{5} = \frac{15}{4}$	Division is not associative for rational numbers.	<p>pupils are divided into heterogeneous groups and given different number triplets to check associativity in Rationals under different operations</p> <table border="1" data-bbox="1318 857 1835 1123"> <thead> <tr> <th>Additive Identity</th> <th>Multiplicative Identity</th> </tr> </thead> <tbody> <tr> <td>Used for addition operation.</td> <td>Used for multiplication operation.</td> </tr> <tr> <td>Given by: <math>p + 0 = p = 0 + p</math></td> <td>Given by: <math>p \times 1 = p = 1 \times p</math></td> </tr> <tr> <td>0 is the identity element</td> <td>1 is the identity element</td> </tr> <tr> <td>For example, <math>77 + 0 = 77</math>, <math>-77 + 0 = -77</math></td> <td>For example, <math>77 \times 1 = 77</math>, <math>-77 \times 1 = -77</math></td> </tr> </tbody> </table>	Additive Identity	Multiplicative Identity	Used for addition operation.	Used for multiplication operation.	Given by: $p + 0 = p = 0 + p$	Given by: $p \times 1 = p = 1 \times p$	0 is the identity element	1 is the identity element	For example, $77 + 0 = 77$ , $-77 + 0 = -77$	For example, $77 \times 1 = 77$ , $-77 \times 1 = -77$	Each student in the group participates in the activity and learns the concept of associativity and role of 0 and 1
LHS	RHS	Result																										
$\left(\frac{1}{5} + \frac{2}{7}\right) + \frac{1}{3} = \frac{86}{105}$	$\frac{1}{5} + \left(\frac{2}{7} + \frac{1}{3}\right) = \frac{86}{105}$	The values are equal and they satisfy the condition.																										
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SUMMARY	Teacher once again writes important key words and tabulates the properties of Rationals and asks children to note down and adopt.	Pupils will note down and read the summary in groups	Every individual reads the summary and notes it down and adopts the procedure																									
ASSESSMENT	Teacher gives some questions from Try These sections of pg no: 9 and asks children to solve those sums	Every group will do the sums by discussion among	Every individual solves the sums on their own																									

PRACTICE PERIODS: 8 to 14	MULTIPLICATION OF INTEGERS, MULTIPLICATION OF A POSITIVE AND A NEGATIVE INTEGER, MULTIPLICATION OF TWO NEGATIVE INTEGERS		
CONCEPTS/STEPS	TEACHER ACTIVITY (I DO)	GROUP ACTIVITY (WE DO)	INDIVIDUAL ACTIVITY ( YOU DO )
KEY WORDS READING	Teacher writes the key words from previous class's teaching period and asks children to read and write them in note books * Associativity * Identity * Inverse	Whole class activity : one child comes to the board and reads the key words loudly and the remaining class follows.	Every child comes to the board and reads the key words and notes them down in their note books
SIMILAR LINES READING	Teacher performs some operations on Rational Numbers and cites the name of the property involved in them and asks children to frame some more by watching similar lines  $\left(\frac{2}{3} + \frac{1}{2}\right) + \frac{3}{4} \neq \frac{2}{3} + \left(\frac{1}{2} + \frac{3}{4}\right)$ Associativity is not satisfied in rationals  $-\frac{15}{8} \times 1 = 1 \times \frac{-15}{8} = \frac{-15}{8}$ 1 is the multiplicative identity in Rationals	Each group watches the similar lines and frames some more	Every individual frames some more statements by watching the similar lines
SUMMARY/ SYNOPSIS	Teacher once again writes important key words tabular form of properties of rationals and asks children to note down and adopt.	Pupil groups will read and adopt the procedure	Teacher focuses on every individual so that each one learns properties in successive
WRITING/ EDITING	Teacher gives some questions from Try These sections of pg no: 9 and asks children to solve those sums and teacher checks the writings of children	One group will check the writings of the other and vice versa	upcoming practice sessions

TEACHING PERIOD : 3	DISTRIBUTIVITY OF MULTIPLICATION OVER ADDITION FOR RATIONAL NUMBERS		
CONCEPTS/STEPS	TEACHER ACTIVITY ( I DO )	GROUP ACTIVITY ( WE DO )	INDIVIDUAL ACTIVITY ( YOU DO )
KEY WORDS	Brain storming session involving children with key words * Distributivity of multiplication over addition	* Students read the key words and answer the	Every Pupil will read and write the key words in their note
CONCEPTUAL UNDERSTANDING	<p>Teacher demonstrates the concept of distributivity of multiplication over addition using some illustrations and induces the distributivity law from the inferences</p> <p>if a,b,c are any three rational numbers then</p> $a \times (b+c) = (a \times b) + (a \times c)$  <p>Let <math>a \times (b+c) = \frac{3}{4} \times \left( \frac{-2}{3} + \frac{3}{7} \right) = \frac{3}{4} \times \left[ \frac{(-2 \times 7) + (3 \times 3)}{21} \right]</math>  <math>= \frac{3}{4} \times \left[ \frac{-14+9}{21} \right] = \frac{3}{4} \times \frac{-5}{21} = \frac{-5}{4 \times 7} = \frac{-5}{28} \dots(1)</math></p> <p><math>(a \times b) + (a \times c) = \left( \frac{3}{4} \times \frac{-2}{3} \right) + \left( \frac{3}{4} \times \frac{3}{7} \right)</math>  <math>= \frac{-6}{12} + \frac{9}{28} = \frac{(-6 \times 7) + (9 \times 3)}{84} = \frac{-42 + 27}{84} = \frac{-15}{84} = \frac{-5}{28}</math></p> <p><math>(a \times b) + (a \times c) = \frac{-5}{28} \dots(2)</math></p>	Hetrogeneous groups are created and different numbers are given and were asked to check the distributivity with them in rational numbers	Every child participates in the learning activity and understands the concept of distributivity
SUMMARY	Teacher writes the summary showing how to prove distributivity in rational numbers on the black board and asks children to read write and note down	pupils will note down and read the summary in groups	every individual reads the summary and notes it down and adopts the procedure
ASSESSMENT	Teacher gives some questions from exercise 1.1 and asks children to solve those sums	every group will do the sums by discussion among each other	every individual solves the sums on their own

PRACTICE PERIODS: 15 to 21		DISTRIBUTIVITY OF MULTIPLICATION OVER ADDITION FOR RATIONAL NUMBERS	
CONCEPTS/STEPS	TEACHER ACTIVITY (I DO)	GROUP ACTIVITY (WE DO)	INDIVIDUAL ACTIVITY ( YOU DO )
KEY WORDS READING	Teacher writes the key words from previous class's teaching period and asks children to read and write them in note books * Distributivity of multiplication over addition	Whole class activity : one child comes to the board and reads the key words loudly and the remaining class follows.	Every child comes to the board and reads the key words and notes them down in their note books
SIMILAR LINES READING	Teacher verifies the distributivity of rationals in a set of numbers and asks children to verify in some more different numbers watching these similar lines  $a \times (b + c) = \frac{-1}{2} \times \left( \frac{2}{3} + \left( \frac{-5}{6} \right) \right) = \frac{-1}{2} \times \left( \frac{(2 \times 2) + (-5 \times 1)}{6} \right)$ $= \frac{-1}{2} \times \left( \frac{4 + (-5)}{6} \right) = \frac{-1}{2} \times \left( \frac{-1}{6} \right)$ $a \times (b + c) = \frac{1}{12} \quad \dots(1)$ $(a \times b) + (a \times c) = \left( \frac{-1}{2} \times \frac{2}{3} \right) + \left( \frac{-1}{2} \times \left( \frac{-5}{6} \right) \right)$ $= \frac{-2}{6} + \frac{5}{12} = \frac{(-2 \times 2) + 5 \times 1}{12} = \frac{-4 + 5}{12}$ $(a \times b) + (a \times c) = \frac{1}{12} \quad \dots(2)$	Each group will read the similar lines and will frame some more by discussion	Every Individual prepares their own similar lines using the lines prepared by the teacher
SUMMARY/ SYNOPSIS	Teacher once again writes important key words and table of properties and asks children to read ,note down and adopt.	Pupil groups will read the table of properties and utilize	Teacher focuses on every individual so that each one knows and adopts the different
WRITING/ EDITING	Teacher asks children to solve the sums of exercise 1.1 on their own and teacher checks the writings of children	One group will check the writings of the other and vice versa	properties in successive upcoming practice sessions